## ECTS catalog with learning outcomes University of Montenegro

Faculty of Science and Mathematics / MATHEMATICS AND COMPUTER SCIENCE / NUMERICAL ANALYSIS

| Course: | NUMERICAL ANALYSIS |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Course ID | Course status | Semester | ECTS credits | Lessons (Lessons+Exer cises+Laboratory) |
| 502 | Mandatory | 5 | 5 | $2+2+0$ |
| Programs | MATHEMATICS AND COMPUTER SCIENCE |  |  |  |
| Prerequisites | None. |  |  |  |
| Aims | The aim of the course is for students to adopt and master the basics of mathematical analysis: limit theory, elements of differential and integral calculus and the theory of series. |  |  |  |
| Learning outcomes | On successful completion of the course, students will be able to: 1 . Define the basic notions of mathematical analysis 1: the set of real numbers, limit of a sequence and function, differentiability of a function, derivative and indefinite integral on an interval. 2. State the basic properties of the set of real numbers. 3. Derive basic propositions in limit theory and differential calculus, determine when a sequence or function has a limit, or when the function is continuous or differentiable. 4. Examine and associate properties of functions of a real variable using differential calculus. 5. Apply the acquired knowledge to solving different tasks related to the stated content of mathematical analysis. 6. Apply the acquired knowledge to solving real tasks and problems. |  |  |  |
| Lecturer / Teaching assistant | Prof. dr Žarko Pavićević -lecturer, Lazar Obradović - teaching assistant |  |  |  |
| Methodology | Lectures, exercises, homework assignments, consultations, written exams. |  |  |  |
| Plan and program of work |  |  |  |  |
| Preparing week | Preparation and registration of the semester |  |  |  |
| I week lectures | Introducing students to basic topics studied in this course. |  |  |  |
| I week exercises | Introducing students to basic topics studied in this course. |  |  |  |
| II week lectures | The set of real numbers - axiomatic construction. |  |  |  |
| Il week exercises | The set of real numbers - axiomatic construction. |  |  |  |
| III week lectures | Completeness principles of the set of real numbers. |  |  |  |
| III week exercises | Completeness principles of the set of real numbers. |  |  |  |
| IV week lectures | Theory of convergent sequences. |  |  |  |
| IV week exercises | Theory of convergent sequences. |  |  |  |
| $\checkmark$ week lectures | Bolzano's and Cauchy's theorem for sequences. Banach fixed-point theorem. |  |  |  |
| V week exercises | Bolzano's and Cauchy's theorem for sequences. Banach fixed-point theorem. |  |  |  |
| VI week lectures | Topology on the set of real numbers. |  |  |  |
| VI week exercises | Topology on the set of real numbers. |  |  |  |
| VII week lectures | Study break |  |  |  |
| VII week exercises | Study break |  |  |  |
| VIII week lectures | Limit of a function. Continuity of a function at a point. |  |  |  |
| VIII week exercises | Limit of a function. Continuity of a function at a point. |  |  |  |
| IX week lectures | Basis of a set. Convergence and continuity of a function with regard to the basis of the set. |  |  |  |
| IX week exercises | Basis of a set. Convergence and continuity of a function with regard to the basis of the set. |  |  |  |
| $X$ week lectures | Global properties of functions which are continuous on a closed interval. First written exam |  |  |  |
| $X$ week exercises | Global properties of functions which are continuous on a closed interval. First written exam |  |  |  |
| XI week lectures | Uniform continuity of functions |  |  |  |
| XI week exercises | Uniform continuity of functions |  |  |  |
| XII week lectures | Differentiability of a function at a point. Derivative. Higher order derivatives. |  |  |  |
| XII week exercises | Differentiability of a function at a point. Derivative. Higher order derivatives. |  |  |  |
| XIII week lectures | Mean value theorem of differential calculus. Bernouli - L'Hopital's rule. Taylor formulas. |  |  |  |


| XIII week exercises |  | Mean value theorem of differential calculus. Bernouli - L'Hopital's rule. Taylor formulas. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| XIV week lectures |  | Monotonicity and extrema of differentiable functions. Convexity of functions. Inflection points. |  |  |  |  |
| XIV week exercises |  | Monotonicity and extrema of differentiable functions. Convexity of functions. Inflection points. |  |  |  |  |
| XV week lectures |  | Examining properties and drawing the graph of a function. Second written exam |  |  |  |  |
| XV week exercises |  | Examining properties and drawing the graph of a function. Second written exam |  |  |  |  |
| Student workload |  | 10 credits $\times 30$ hours $=300$ hours |  |  |  |  |
| Per week |  |  | Per semester |  |  |  |
| 5 credits $\times \mathbf{4 0} / \mathbf{3 0}=\mathbf{6}$ hours and $\mathbf{4 0}$ minuts <br> 2 sat(a) theoretical classes <br> 0 sat(a) practical classes <br> 2 excercises <br> 2 hour(s) i 40 minuts <br> of independent work, including consultations |  |  | Classes and final exam: <br> $\mathbf{6}$ hour(s) i $\mathbf{4 0}$ minuts $\mathbf{x} \mathbf{1 6 = 1 0 6}$ hour(s) i $\mathbf{4 0}$ minuts <br> Necessary preparation before the beginning of the semester <br> (administration, registration, certification): <br> $\mathbf{6}$ hour(s) i $\mathbf{4 0}$ minuts $\times 2=13$ hour(s) i $\mathbf{2 0}$ minuts <br> Total workload for the subject: <br> $5 \times 30=150$ hour(s) <br> Additional work for exam preparation in the preparing exam period, including taking the remedial exam from 0 to 30 hours (remaining time from the first two items to the total load for the item) <br> 30 hour(s) i 0 minuts <br> Workload structure: $\mathbf{1 0 6}$ hour(s) i $\mathbf{4 0}$ minuts (cources), $\mathbf{1 3}$ hour(s) i 20 minuts (preparation), $\mathbf{3 0}$ hour(s) i $\mathbf{0}$ minuts (additional work) |  |  |  |
| Student obligations |  |  | Students are required to attend classes, do the homework assignments and take all exams. |  |  |  |
| Consultations |  |  | 1 hour a week (lectures) + 1 hour a week (exercises) |  |  |  |
| Literature |  |  | V. I. Gavrilov,,Ž. Pavićević, Matematička analiza I, I.M. Lavrentjev, R. Šćepanović, Zbirka zadataka iz mat. analize I |  |  |  |
| Examination methods |  |  | 4 homework assignments, 2 points each ( 8 points in total). 2 points for attendance. 2 written exams, 20 points each ( 40 points in total). Final exam, 50 points. Students who collect at least 51 points pass the course. |  |  |  |
| Special remarks |  |  |  |  |  |  |
| Comment |  |  |  |  |  |  |
| Grade: | F | E | D | C | B | A |
| Number of points | less th points | greater than or equal to 50 points and less than 60 points | greater than or equal to 60 points and less than 70 points | greater than or equal to 70 points and less than 80 points | greater than or equal to 80 points and less than 90 points | greater than or equal to 90 points |

